

10. Express each of the following numbers as the sum of three odd primes. (4)

a. 21

$$\star 21 \rightarrow 3 + 5 + 13$$

$$\star 21 \rightarrow 3 + 7 + 11$$

c. 53

$$\star 53 \rightarrow 13 + 17 + 23$$

$$53 \rightarrow 7 + 17 + 29$$

b. 31

$$\star 31 \rightarrow 3 + 5 + 23$$

$$31 \rightarrow 7 + 11 + 13$$

d. 61

$$\star 61 \rightarrow 7 + 13 + 41$$

$$\star 61 \rightarrow 15 + 17 + 29$$

Ex 3.3

2. Using divisibility tests, determine which of the following numbers are divisible by 4; by 8:

b. 726352

$$\star 726\overline{35}2 \rightarrow 52 \text{ is divisible by } 4$$

$$726\overline{35}2 \rightarrow 352 \text{ is divisible by } 8$$

Ans: 726352 \rightarrow Divisible by 4 and 8.

d. 6000

$$\star \overline{6000} \rightarrow \text{divisible by } 4$$

$$\overline{6000} \rightarrow \text{divisible by } 8$$

Ans: 6000 \rightarrow Divisible by 4 and 8

f. 14560

$$\star \overline{14560} \rightarrow 60 \text{ is divisible by } 4$$

$$\overline{14560} \rightarrow 560 \text{ is divisible by } 8$$

Ans: 14560 \rightarrow Divisible by 4 and 8

g. 21084

$$\star \overline{21084} \rightarrow 84 \text{ is divisible by } 4$$

$$\overline{21084} \rightarrow \text{not divisible by } 8$$

A: 21084 \rightarrow Divisible by 4
not divisible by 8

h. 31795072

$$\star \overline{31795072} \rightarrow 72 \text{ is divisible by } 4$$

$$\overline{31795072} \rightarrow \text{Divisible by } 8$$

\star A: 31795072 \rightarrow Divisible by 4 and 8.

j. 2150

$$\star \overline{2150} \rightarrow 50 \text{ is not divisible by } 4$$

$$\overline{2150} \rightarrow 150 \text{ is not divisible by } 8$$

\star A: 2150 \rightarrow not divisible by 4 and 8.

3. Using divisibility tests, determine which of following numbers are divisible by 6:

a. 297144

$$\star \overline{297144} \rightarrow 4 \text{ is divisible by } 2$$

$$297144 \rightarrow 2 + 9 + 7 + 1 + 4 + 4$$

$$\rightarrow 27 \rightarrow \text{divisible by } 3$$

$$297144 \rightarrow \text{Divisible by } 2 \text{ and } 3$$

\star Ans 297144 \rightarrow Divisible by 6.

f. 438750 ⑥
 438750 \rightarrow Divisible by 2
 438750 $\rightarrow 4+3+8+7+5+0$
 $\rightarrow 27 \rightarrow$ Divisible by 3
 438750 \rightarrow Divisible by 2 and 3
 Ans: 438750 \rightarrow Divisible by 6.

g. 1790184
 1790184 \rightarrow Divisible by 2
 1790184 $\rightarrow 1+7+9+0+1+8+4$
 $\rightarrow 30 \rightarrow$ Divisible by 3
 1790184 \rightarrow Divisible by 2 and 3
 Ans: 1790184 \rightarrow Divisible by 6

b. 1258
 1258 \rightarrow Divisible by 2
 1258 $\rightarrow 1+2+5+8$
 $\rightarrow 16 \rightarrow$ not divisible by 3
 1258 \rightarrow Divisible by 2, not divisible by 3
 Ans: 1258 \rightarrow not divisible by 6.

d. 61233
 61233 \rightarrow not divisible by 2
 61233 $\rightarrow 6+1+2+3+3$
 $\rightarrow 15 \rightarrow$ Divisible by 3
 61233 \rightarrow not divisible by 2, divisible by 3
 Ans: 61233 \rightarrow not divisible by 6.

h. 12583
 * 12583 \rightarrow not divisible by 2
 12583 $\rightarrow 1+2+5+8+3$
 $\rightarrow 19 \rightarrow$ not divisible by 3
 12583 \rightarrow not divisible by 2 and 3
 Ans: 12583 \rightarrow not divisible by 6.

4. Using divisibility tests, determine which of the following numbers are divisible by 11.

a. 5445
 * Sum of the digits
 odd places [from the right]
 5+4 $\rightarrow 9$
 even places
 4+5 $\rightarrow 9$
 Difference $\rightarrow 9 - 9 = 0$

Ans: 5445 \rightarrow Divisible by 11.

e. 10000001

10000001

* Sum of the digits
 Odd places
 1+0+0+0 $\rightarrow 1$
 even places
 0+0+0+1 $\rightarrow 1$

* Difference $\rightarrow 1 - 1$
 $\rightarrow 0$

* 10000001 \rightarrow Divisible by 11.

b. 10824

1 0 8 2 4

* Sum of the digits

odd places

$$4 + 8 + 1 \rightarrow 13$$

even places

$$2 + 0 \rightarrow 2$$

$$\text{Difference} \rightarrow 13 - 2$$

$$\rightarrow 11$$

* Ans 10824 \rightarrow Divisible by 11.

c. 7138965

7 1 3 8 9 6 5

* Sum of the digits

odd places

$$5 + 9 + 3 + 7 \rightarrow 24$$

even places

$$6 + 8 + 1 \rightarrow 15$$

$$\text{Difference} \rightarrow 24 - 15$$

$$\rightarrow 9$$

Ans: 7138965 \rightarrow not divisible by 11.

8

5. Write the smallest digit and the greatest 9 digit in the blank space of each of the following numbers so that the number formed is divisible by 3:

b. 4765 - 2

$$\star 4 + 7 + 6 + 5 + 2 = 24$$

$$= 24 \text{ is divisible by } 3$$

$$\star 4765 \underline{0} 2$$

$$= \text{divisible by } 3$$

$$\star : 4765 \underline{9} 2$$

$$= 24 + 9$$

$$= 33 \rightarrow \text{Divisible by } 3$$

Ans: * Smallest digit $\rightarrow 0 \rightarrow 4765 \underline{0} 2$.

* Greatest digit $\rightarrow 9 \rightarrow 4765 \underline{9} 2$

6. Write a digit in the blank space of each of the following numbers so that the number formed is divisible by 11

a. 92 - 389

9 2 - 3 8 9

$$9 + 3 + 2 \rightarrow 14$$

$$8 + - + 9 \rightarrow 17$$

$$8 + \underline{8} + 9 \rightarrow 17 + 8$$

$$\rightarrow 25$$

$$\rightarrow 25 - 14$$

$$\rightarrow 11 \rightarrow \text{divisible by } 11$$

Ans: 92 8 389

b. 8 - 9484

$$\textcircled{8} - \textcircled{9}4 \textcircled{8}4$$

$$4 + 4 + - = 8$$

$$8 + 9 + 8 = 25$$

$$4 + 4 + \underline{6} = 8 + 6$$

$$= 14$$

$$= 25 - 14$$

$$= 11 \rightarrow \text{Divisible by 11}$$

Ans: 8 6 9484.

Ex 3.4

1. Find the common factors of :

a. 20 and 28

* Factors:

$$20 \rightarrow \begin{matrix} 1 \times 20 \\ 2 \times 10 \\ 4 \times 5 \end{matrix}$$

$$28 \rightarrow \begin{matrix} 1 \times 28 \\ 2 \times 14 \\ 4 \times 7 \end{matrix}$$

$$20 \rightarrow \underline{1, 2, 4}, 5, 10, 20$$

$$28 \rightarrow \underline{1, 2, 4, 7, 14}, 28$$

Common factors $\rightarrow 1, 2, 4$

A $\rightarrow 1, 2, 4.$

d. 56 and 120

* Factors:

$$56 \rightarrow \begin{matrix} 1 \times 56 \\ 2 \times 28 \\ 4 \times 14 \\ 7 \times 8 \end{matrix}$$

$$120 \rightarrow \begin{matrix} 1 \times 120 \\ 2 \times 60 \\ 3 \times 40 \\ 4 \times 30 \\ 5 \times 24 \\ 6 \times 20 \\ 8 \times 15 \\ 10 \times 12 \end{matrix}$$

$$56 \rightarrow \textcircled{1}, \textcircled{2}, \textcircled{4}, 7, \textcircled{8}, 9, 14, 28, 56$$

$$120 \rightarrow \textcircled{1}, \textcircled{2}, 3, \textcircled{4}, 5, 6, \textcircled{8}, 10, 12, 15, 20, 24, 30, \textcircled{40}, 60, 120$$

Common $\rightarrow 1, 2, 4, 8.$

factors

A $\rightarrow 1, 2, 4, 8$

2. Find the common factors of :

b. 5, 15 and 25

Factors:

$$5 \rightarrow 1 \times 5$$

$$15 \rightarrow \begin{matrix} 1 \times 15 \\ 3 \times 5 \end{matrix}$$

$$25 \rightarrow \begin{matrix} 1 \times 25 \\ 5 \times 5 \end{matrix}$$

$$5 \rightarrow \textcircled{1}, \textcircled{5}$$

$$15 \rightarrow \textcircled{1}, 3, \textcircled{5}, 15$$

$$25 \rightarrow \textcircled{1}, \textcircled{5}, 25$$

Common factors $\rightarrow 1, 5.$

3. Find first three common multiples of :

b. 12 and 18

Multiples of 12

12, 24, 36, 48, 60, 72, 84, 96, 108, 120.